

# Pragmatism vs. Elegance

comparing two approaches to Simple Power Analysis on AES

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# AES: Advanced Encryption Standard

- Symmetric-key block cipher
- Key size: **128**, 192, and 256 bits
- Block size: **128** bits
  
- Announced by the NIST as U.S. FIPS PUB 197 on 26.11.2001

# Classic Simple Power Analysis (SPA) Attacks

- Classic SPA attacks can be compared to brute-force
- Side-channel information makes this approach feasible against modern-day ciphers
- Most common leakage models: **8-bit Hamming weight** and Hamming distance

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- Side-channel information makes this approach feasible against modern-day ciphers
- Most common leakage models: **8-bit Hamming weight** and Hamming distance
- In practice, side-channel information cannot be measured perfectly (i.e., **noise**)
  - ▶ average over a few measurements
  - ▶ drop information with high error probability
  - ▶ encapsulate side-channel information as a set of (consecutive) possible values, **always containing the correct value**

# Classic SPA Attacks on AES

## Mangard's Attack

- Targets Key Schedule
- 5 consecutive round keys
- Side-channel information: **correct HW value** or **no information at all**

## ASCA Attack

- Targets Encryption Rounds
- All encryption rounds
- Side-channel information: **sets of up to 3 possible HW values**

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- 5 consecutive round keys
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- Result: Reduced keyspace

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- All encryption rounds
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Our approach:

- Combine information of Encryption Rounds *and* Key Schedule of a single round
- Side-channel information: sets of up to **5** possible values



# The AES Encryption algorithm

## Encryption Rounds

- Initial Round
  - ▶ AddRoundKey
- Intermediate Rounds
  - ▶ SubBytes
  - ▶ ShiftRows
  - ▶ MixColumns
  - ▶ AddRoundKey
- Final Round
  - ▶ SubBytes
  - ▶ ShiftRows
  - ▶ AddRoundKey.

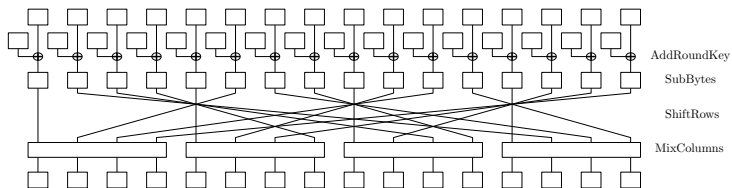
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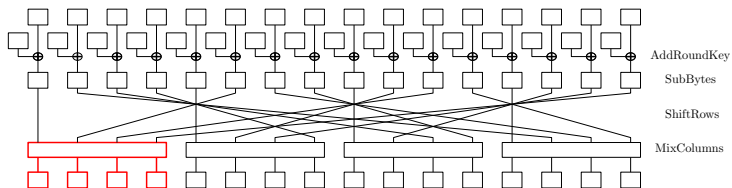
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## Attacking the Encryption Round Function



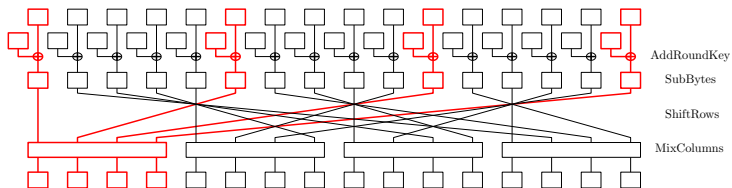
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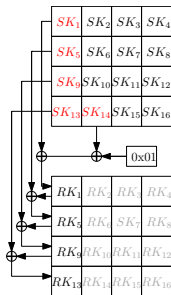
# The AES Encryption algorithm

## Key Schedule

- Represent the secret key as a set of 4-byte words
- Derive one new word at a time from two previous words
- Operations:
  - ▶ Circular shift of word bytes
  - ▶ S-box lookup
  - ▶ XOR-ing with a round constant
  - ▶ XOR-ing two words

# The AES Encryption algorithm

## Attacking the Key Expansion Function



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## Attacking the Key Expansion Function

$SK_1$	$SK_2$	$SK_3$	$SK_4$
$SK_5$	$SK_6$	$SK_7$	$SK_8$
$SK_9$	$SK_{10}$	$SK_{11}$	$SK_{12}$
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# Results

## Previous results

**Mangard's Attack** (attacking 5 consecutive Round Keys, 1000 experiments)

HW used	100%	95%	50%
key space	11	16.5	$1.7 \cdot 10^{12}$
time	5m30s	5m	5h

**ASCA Attack success rate** (known PT and CT, 100 experiments)

# rounds	2	4	6
consecutive	0%	100%	100%
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(Using leaks from one encryption round and one round key. The PT is known. Averaged over 500 experiments)

Set size	Encryption only		Key Schedule only		Combined	
	Key space	Execution time	Key space	Execution time	Key space	Execution time
1	1	0.02 s	$2^{58}$	0.4 s	1	0.03 s
2	$2^{20}$	2.9 s	$2^{74}$	5 s	$2^{12}$	27 s
3	$2^{48}$	73.9 s	$2^{95}$	10 s	$2^{13}$	4 m
4	$2^{64}$	27 m	$2^{106}$	30 s	$2^{52}$	35 m
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Moreover, our attack gives a clear indication of the key space that needs to be brute-forced

# Thank you for your attention